

SUPPLEMENTARY MATERIAL TO
**Copper ions biosorption onto bean shells: Kinetics, equilibrium
and process optimization studies**

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MODELS

The pseudo-first order kinetic model is given by:¹

$$\frac{dq(t)}{dt} = k_1(q_e - q(t)) \quad (\text{S-1})$$

where: $q(t)$ – is the adsorbent capacity defined as the mass of the adsorbed metal per unit mass of the adsorbent (mg g^{-1}) at time t ; q_e – is the adsorption capacity defined as mass of the adsorbed metal per unit mass of the adsorbent (mg g^{-1}) at equilibrium; k_1 – is the adsorption rate constant for the pseudo-first order kinetic model (min^{-1}).

Integrating the Eq. (S-1), it follows:

$$\log(q_e - q(t)) = \log(q_e) - \frac{k_1}{2,303} \times t \quad (\text{S-2})$$

The pseudo-second order kinetic model can be expressed as:²

$$\frac{dq(t)}{dt} = k_2(q_e - q(t))^2 \quad (\text{S-3})$$

where: $q(t)$ - is the adsorbent capacity defined as the mass of the adsorbed metal per unit mass of the adsorbent (mg g^{-1}) at time t ; q_e - is the adsorption capacity defined as mass of the adsorbed metal per unit mass of the adsorbent (mg g^{-1}) at equilibrium; k_2 - is the adsorption rate constant for the pseudo-second order kinetic model ($\text{g mg}^{-1} \text{min}^{-1}$).³

The linear form of Eq. (S-3) is:

$$\frac{1}{(q_e - q(t))} = \frac{1}{q_e} + k_2 t \quad (\text{S-4})$$

The intraparticle diffusion kinetic model is given as:¹

$$q(t) = k_i t^{1/2} + C_i \quad (\text{S-5})$$

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where: $q(t)$ - is the adsorption capacity defined as the mass of the adsorbed metal per unit mass of the adsorbent (mg g^{-1}) at time t ; k_i - is the internal particle diffusion rate constant ($\text{mg g}^{-1} \text{min}^{-0.5}$); and C_i - is a constant that provides insight into the thickness of the boundary layer. If the C_i value is higher, the boundary layer effect is greater, so the effect of surface adsorption in controlling the process speed is greater (mg g^{-1}).

Elovich kinetic model is given in the following form:¹

$$\frac{dq(t)}{dt} = \alpha e^{-\beta q(t)} \quad (\text{S-6})$$

where: α - is the starting adsorption rate ($\text{mg g}^{-1} \text{min}^{-1}$); β - is the parameter that expresses the degree of surface coverage and activation energy for chemisorption (g mg^{-1}); $q(t)$ - is the adsorption capacity defined as the mass of the adsorbed metal per unit mass of the adsorbent (mg g^{-1}) at time t .

The Langmuir model can be expressed as:¹

$$q_e = \frac{q_m K_L C_e}{1 + K_L C_e} \quad (\text{S-7})$$

where C_e - is the equilibrium concentration of metal ions (mg dm^{-3}); q_e - is the equilibrium adsorption capacity (mg g^{-1}); q_m - is the maximum adsorption capacity (mg g^{-1}); and K_L - is the Langmuir equilibrium constant ($\text{dm}^3 \text{g}^{-1}$).

Linearizing the Eq. (S-7) the following is obtained:

$$C_e/q_e = \frac{1}{K_L q_m} + \frac{1}{q_m} C_e \quad (\text{S-8})$$

This model can be expressed as:¹

$$q_e = K_f C_e^{1/n} \quad (\text{S-9})$$

where C_e - is the equilibrium concentration of copper ions in the solution (mg dm^{-3}); q_e - is the adsorbent capacity defined as mass of the adsorbed metal per unit mass of the adsorbent (mg g^{-1}) at equilibrium; K_f - is the Freundlich equilibrium constant ($(\text{mg g}^{-1}) (\text{dm}^3 \text{mg}^{-1})^{1/n}$); and $1/n$ - is the coefficient of heterogeneity in the Freundlich adsorption isotherm equation.

Linear form of Eq. (S-9) is:

$$\log q_w = \log K_f + \frac{1}{n} \log C_e \quad (\text{S-10})$$

The Temkin isotherm model is given as:

$$q_e = B \ln(K_T C_e) \quad (\text{S-11})$$

where: $B = RT/b$ - is the Temkin constant, which refers to the adsorption heat (J mol^{-1}); b - is the variation of adsorption energy (J mol^{-1}); R - is the universal gas constant ($\text{J mol}^{-1} \text{K}^{-1}$); T - is the temperature (K); K_T - is the Temkin equilibrium constant ($\text{dm}^3 \text{g}^{-1}$); q_e - is the adsorption capacity (mg g^{-1}) at equilibrium; and C_e - is the equilibrium concentration of metal ions in the solution (mg dm^{-3}).¹

Linear form of Eq. (S-11) is:

$$q_e = B \ln K_T + B \ln C_e \quad (\text{S-12})$$

The correlation between the following independent variables: linear ($\beta_1, \beta_2, \beta_3$), quadratic ($\beta_{11}, \beta_{22}, \beta_{33}$), interaction terms ($\beta_{12}, \beta_{13}, \beta_{23}$), and the response (Y), was described by fitting the following polynomial equation:⁴

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_3 + \beta_{11} X_1 X_1 + \beta_{22} X_2 X_2 + \beta_{33} X_3 X_3 + \beta_{12} X_1 X_2 + \beta_{13} X_1 X_3 + \beta_{23} X_2 X_3 \quad (\text{S-13})$$

The obtained results are displayed in Table VI. The biosorption of copper ions onto bean shells was expressed using the following equation:

$$Y = 31,76 + 6,88X_1 - 28,56X_2 - 1,46X_3 - 3,71X_1 \cdot X_1 + 10,42X_2 \cdot X_2 + 0,69X_3 \cdot X_3 - 16,06X_1 \cdot X_2 + 6,40X_1 \cdot X_3 + 4,57X_2 \cdot X_3 \quad (\text{S-14})$$

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